

The importance of RID and P Vs h^n curves on indentation studies of TiN films deposited onto M2 and 304L steels

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Abstract

A hardness study of *TiN* films onto *M2* and *304L* steels applied by *PAPVD* was conducted in this work. Instrumented indentation and hardness equipments allow to asses this property. Crack patterns produced during these tests were correlated with this information. In addition, from the *P-h/t* (Load-displacement/film's thickness) plots, called *Relative Indenter Displacement* plots, and *P-hⁿ* plots important information was obtained about the capacity of these systems for supporting load. Both graphics showed to be of great importance for understanding the mechanical response of these systems to indentation.

----- *Key words:* mechanical properties, thin films, indentation, hardness, TiN, PAPVD.

La importancia de las curvas RID y P-hⁿ en los estudios de capas TiN depositadas sobre aceros M2 y 304L

Resumen

En este trabajo se realizó un estudio de la dureza de capas *TiN* aplicadas mediante *PAPVD* depositadas sobre acero *M2* e inoxidable *304L*. Esto se hizo utilizando un equipo de indentación con censado de desplazamiento y equipos de micro y macrodureza convencionales. Los patrones de agrietamiento dejados en la impresión

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se correlacionaron con estas propiedades. Se obtuvo información importante de las curvas $P-h/t$ (Carga-desplazamiento/espesor de la capa), llamadas curvas de desplazamiento relativo del indentador (curvas RID), y de las curvas $P-h'$. Ambas curvas mostraron ser de gran importancia en el entendimiento del comportamiento mecánico de los sistemas estudiados.

----- *Palabras clave:* propiedades mecánicas, capas finas, indentación, dureza, TiN, PAPVD.

Introduction

Indentation tests are nowadays one of the most important tools for the evaluation of mechanical response of films deposited onto hard and soft substrates. In particular, this technique allows to study the hardness (H), elastic modulus (E), toughness (K_C), of the film, and its adherence to substrate [1]. To assess these parameters it is necessary to use both heavy (micro and macro indentation) and small loads (nanoindentation) depending on the studied system.

There are different tip indenter geometries, the more commonly used being the are pyramidal (Berkovich and Vickers) preferred to induce cracks and plastic flow at low loads, also due to the “easiness” to characterize its geometry and to the self similarity characteristics. These sort of indenters are used for the evaluation of H , E and K_C .

Great improvements in technology have permitted to record both small loads and displacements at the same time, and this turns the indentation

test into instrumented indentation test, also know as nanoindentation. The data are usually plotted as P Vs h (figure 1(a)), but recently some researches community have been working in the extraction of more information from nanoindentation data, particularly in coated systems [2-6]. It includes the construction of hardness versus relative indentation depth ($\beta = h$ (depth) / t (film thickness)) or RID plots and $P-h^2$ plots.

Theoretically, modeling bulk materials as rigid perfectly plastic solids, Loubet et al. [7] demonstrated that the data plotted as $P-h^2$, produces for a Vickers indenter a straight line. When a material is composed by a film and substrate, under small loads a coating-dominated response is expected and under large loads the system behavior is dominated by the substrate. Therefore, the $P-h^2$ plot will present straight regions in which the film or substrate dominates the behavior. Transition points named T_c/s and T_s/s respectively (figure 1(b)) limit these regions. Obviously, these transition points also define the points where hardness and elastic modulus corresponds to film or to substrate.

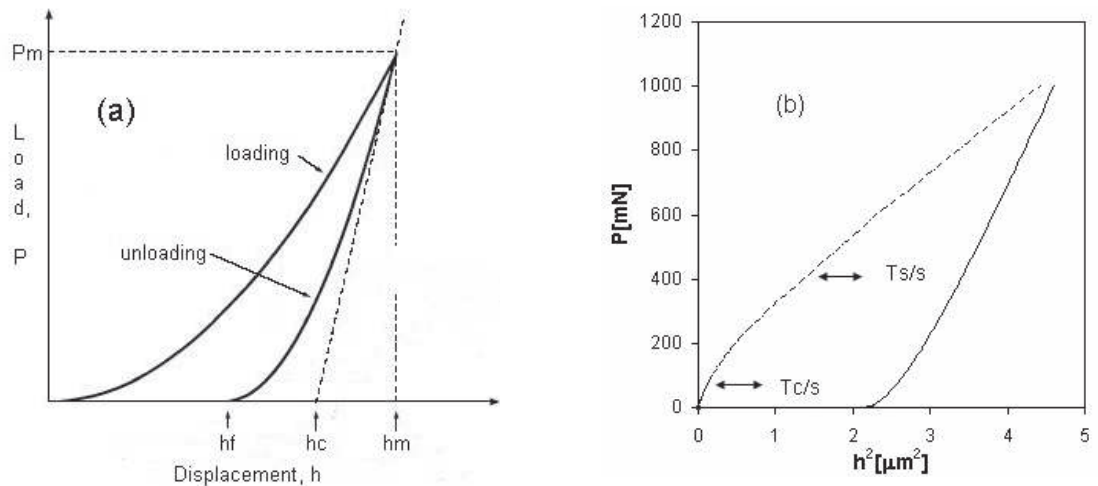


Figure 1 Schematic representation of indentation data. (a) Load-displacement P-h plot, (b) P versus h^2 plot. Arrows indicate the transition point to film dominated behavior (T_c/s) and substrate dominated behavior (T_s/s)

Real pyramidal indenters have some tip roundness, and real materials work hardens. Furthermore, hard films are commonly brittle, and exist the possibility of pile up around the indenter and indentation size effect (*ISE*). The original model of Loubet does not take into account these parameters; therefore one can expect that the behavior of real materials follow a more general expression: $P-h^n$. Thus, the transition points obtained by $P-h^2$ plots could not be appropriate in all cases. Recently proposed Finite Element Models conducted by Bolshakov et al. [8] addressed some of these questions. They demonstrated that maybe the best relation to describe the unload nanoindentation plots are of the form $P-h^m$ where $m \approx 1,5$, even for a flat punch, cone or other indenter geometry, which indicates that this values are due to a complex elastoplastic materials response and not to tip roundness.

In the other hand, *RID* plots (see figure 4) allows to explore the results of hardness and Young's modulus in a spread load range, showing the transition of coated dominated to a coated-substrate and to a substrate dominated system response. These phenomena are associated with the plastic flow on substrate and with cracks induced in hard-brittle coatings which conducts to a stiffness lose until it does not opposes any resistance to the indenter penetration and only transmits load to the substrate.

Due to the importance of *RID* plots, its development is shortly revised.

A model to predict hardness in a coated-substrate system should take into account the surface generation, deformation and mechanical energy involved in the indentation process. Korsunsky et al. [2-6] proposed this sort of model; finding that the measured hardness (H_c) follows equation 1:

$$H_c = H_s + \frac{H_f - H_s}{1 + \alpha\beta^2} \quad (1)$$

Where H_f is the film hardness, H_s the substrate hardness and α depends, among other things, on K_c film and film-substrate interface toughness.

Also $\beta = h/t$ (*RID* parameter) where h is the maximum indentation depth. Plotting H_c Vs *RID* is possible to obtain H_f , H_s , k . This equation had proved to be capable to predict the behavior of widely coated systems [2, 6]. However, the value of 2 that accompanies to β , proved to be quite restrictive and was substituted for a variable parameter k :

$$H_c = H_s + \frac{H_f - H_s}{1 + \alpha\beta^k} \quad (2)$$

Because of the dependence between α and k , a new parameter β_0 was introduced, resulting in an improved equation [6].

$$H_c = H_s + \frac{H_f - H_s}{1 + \left(\frac{\beta}{\beta_0}\right)^k} \quad (3)$$

Where β_0 is called *efficiency parameter*. The meaning of β_0 is understood if in equation 2, $\beta = \beta_0$. Then becomes:

$$\frac{H_c - H_s}{H_f - H_s} = \frac{1}{2} \quad (4)$$

β_0 could be interpreted as the *RID* value at which the improvement in hardness of substrate due to the film presence is of 50% compared with the maximum achievable, or as the *RID* values at which the film efficiency is 50%.

This work studies the mechanical response of *TiN-M2* and *TiN-304L* systems; particularly explore different possibilities to establish the transition points between coated only behavior to coating-substrate T_c/s , and to only substrate behavior T_s/s . Also is explored the capacity of the coated systems to support load, because this could be of great importance to the design of this systems.

Experimental study

Materials and characterization

The substrate materials were cylindrical pieces of *M2* tool steel heat-treated to 59 HRC and

304L stainless steel metallographically polished. Titanium nitride was deposited on both specimen types in a commercial Balzers reactor using an Arc-Plasma Assisted Physical Vapor Deposition (*arc-PAPVD*). The deposition was made at 500 °C, during 2 h until a thickness of about 3 μm was achieved. The microstructure and morphology were assessed by Scanning electron microscopy (*SEM*) in a *JEOL 5900LV microscope* and atomic force microscopy (*AFM*) in a *multitask system Auto Probe CP*. Present phases were assessed by parallel beams X ray diffraction (*XRD*) in a Bruker D8 advanced (Cu Ka, λ = 1,542 Å).

Indentation test

All the specimens were subjected to static indentation with loads between 5 mN and 1.000 mN, applied using a Fischer H100V nanoindenter equipment with Vickers indenter geometry previously calibrated by the linear method [9]. For each load were collected data of at least 5 *well comported* indentations. To obtain results at loads beyond of 1.000 mN conventional micro *Buehler MM3 tester* and macro hardness *Buehler VM7* apparatus were used.

Indentations allowed to obtain the hardness and elastic modulus of films and substrate, and their

variation with the relative indenter displacement. The crack patterns generated during indentation where characterized by *AFM* and *SEM* microscopy.

Experimental results and discussion

Figure 2 shows topography of the films, for both systems *TiN-M2* and *TiN-304L* it looks similar and due to the fabrication process these films grew in a columnar shape of about 13 nm in diameter. The roughness (*Ra*) measured by *AFM* is about 40 nm. *EDS* results show that the films deposited under *M2* substrate are almost estequimetric, contrary to that deposited in *304L*, that are $Ti_{0,66}N_{0,34}$. Figure 3 shows *XRD* results, both systems shows little differences in what respect to texture and residual compressive stresses.

All specimens were made in the same batch, the only difference was the position on the camera, this can cause some diference in the film thickness, but measurements done by meas of *calo-test* indicate that the *304L-TiN* films were almost of the same thickness of *M2-TiN* films, wich is about 3 μm. However, the diference in composition, shows that the substrate plays an important role on the films' growth and could also influence its composition.

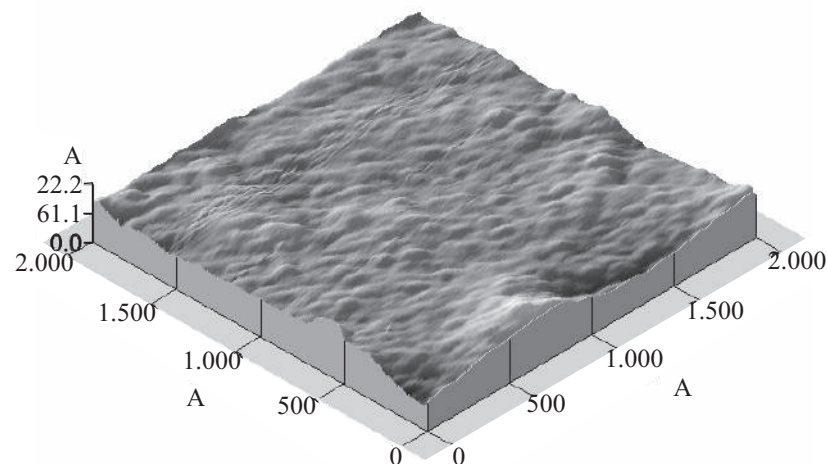


Figure 2 AFM topographic image of a TiN film deposited onto 304L steel

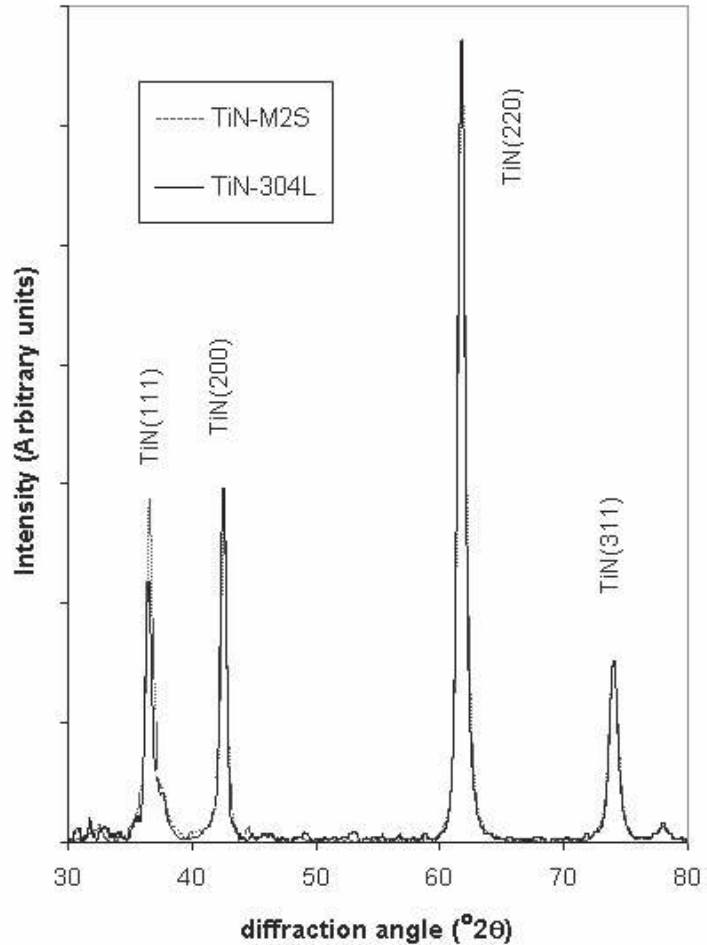


Figure 3 XDR results for TiN films

Figure 4 shows the results of hardness for both systems. This plot known as *Relative Indentation Displacement* (RID) presents four main regions:

R1: For loads under 15 mN ($RID < 0,05$ i. e. depth low than 150 nm), the hardness decreases with the load, also standard deviation is higher.

R2: Between 15 and 50 mN ($0,05 < RID < 0,07$) the hardness has a maximum and stable value of about 25 GPa, the standard deviation had reduced respect to *R1* interval.

R3: $0,07 < RID < 0,4-0,5$ the hardness and its standard deviation diminishes with load.

R4: $RID > 0,4-0,5$ the plot goes to a plateau, reaching a constant value of 7,8 GPa, for *M2-TiN* and to 2,8 GPa for *304L-TiN*, also the standard deviation continuously decreases with load.

The trends of Young's modulus are the same as for hardness, with a maximum value of 400 GPa and a minimum about 200 GPa.

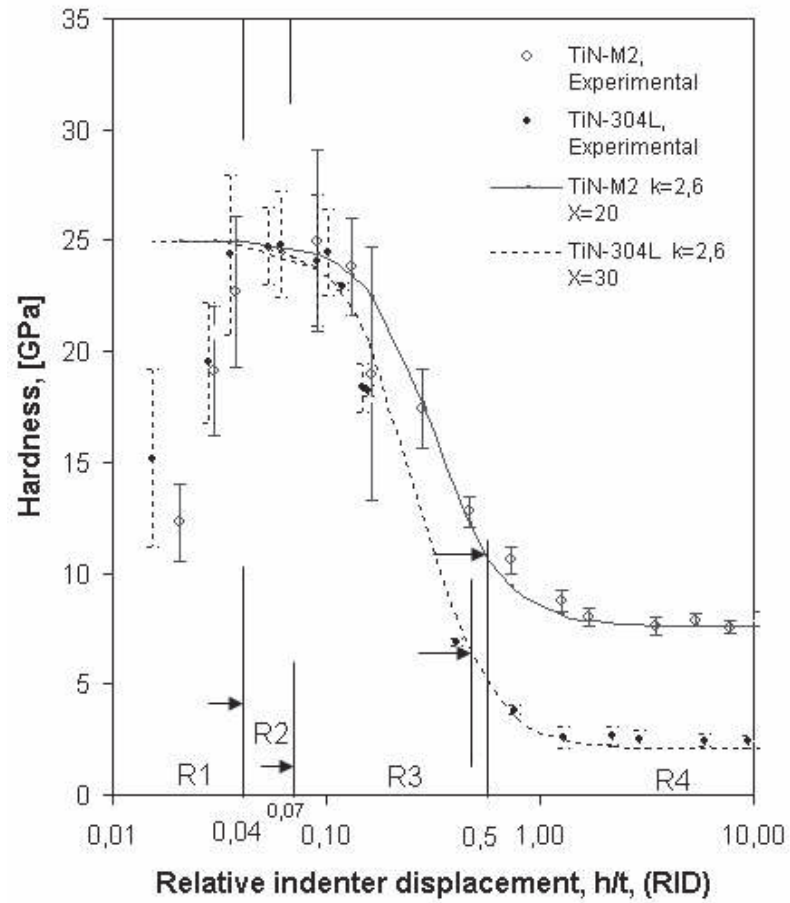


Figure 4 Hardness variation for TiN-M2 and TiN-304L systems with RID parameter (h/t), also shown the adjusts to equation 3

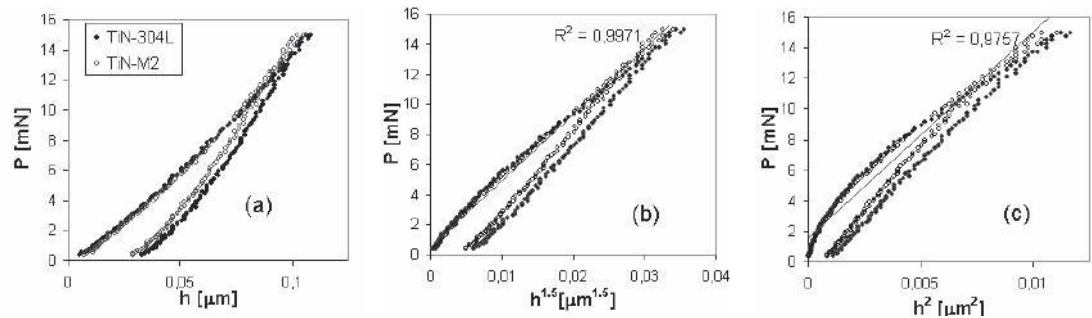


Figure 5 $P-h^{\chi}$ plots for R1 region.

Figure 5 shows $P-h\eta$ plots for $R1$ region. It is difficult to discern if exists some difference in response for each system due to great data dispersion.

The film roughness is about 40 nm, which is in the order of the contact depth, this indicate that in many cases the contact area could be overestimated [10]. The columnar growth of this films produces an opened structure at the top surface, implying that the indenter could penetrate more easily in this region, which is less stiffness than the structure bottom. Therefore the measured hardness increases with load. Other possibilities have been suggested [11], indicating that this loss of hardness and elastic modulus in fact occurs.

$P-h^2$ plots are not straight lines as can be expected (figure 5c), instead they are curves. Many authors had attributed this to the film's surface roughness and the tip roundness that causes a Hertzian contact which is modeled as $P-h^{1.5}$. The indenter tip roundness was estimated about 1,5 μm , which means that until depths about 60 nm contact could be of the Hertzian type. In fact, the behavior of $R1$ region resembles the *Hertzian contact*, because the $P-h^{1.5}$ plot showed on figure 5b is almost linear [12]. It is important to note that the end of $R1$ region is hardly detected whit $P-h^\eta$ plots, but it is easy in RID plots, as shown in figure 4.

However, for the equipment utilized, $P-h^2$ plots seldom are straight line plots, even in bulk materials free of oxide films and plastic hardened

surfaces, instead data acquired by instrumented indentation are best-fitted trough an equation of the form $P-h^\eta$ where η varies between 1,3 and 1,9.

In the same way has been suggested [13] that the unload data can be adjusted to an equation of the form

$$P = k(h - b)^m \tag{5}$$

The constants k , b and m are adjustment parameters, and the m value is associated with tip geometry and is equal to 1, 1,5, 2 for Flat ended-cylindrical punch, paraboloid of revolution and cone respectively. However, recent studies conducted by Bolshakov et al. [8] indicated that the m value is low and nearest to 1,5 due to a complex elastoplastic process during indentation and not only to the tip indenter geometry.

Figure 5 $P-h$, $P-h^2$ and $Ph^{1.5}$ plots for TiN-304L and TiN-M2 systems obtained at 15 mN they show the response in the $R1$ region, correlation coefficients for linear adjustments are shown as $R2$

Figure 6 shows m and η values obtained for soda lime glass, high pure alumina and 304L steel, with $10 < E/H < 91$, values which covers all commonly used engineering materials. It shows that m values are about to 1,5 even for high depths where any influence of tip roundness is insignificant (for more details on the calculation procedure see reference [9]). This result is in agreement with Bolshakov's predictions.

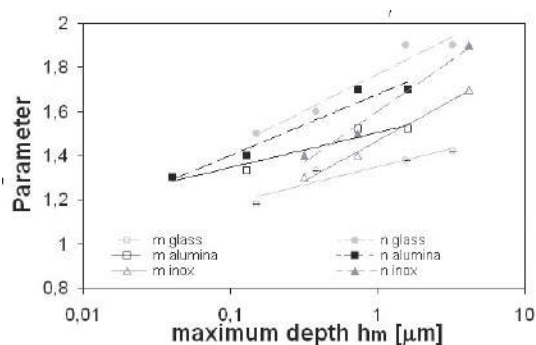


Figure 6 Values of m and η parameters in different bulk materials, glass and alumina are free of oxide and disturbing surface effects, while 304L steel has a strain hardened surface

As was stated above, η values continuously increase with depth between 1,3 and 1,9, and $P-h^2$ plots have lower correlation coefficients than $P-h^n$ plots.

Curiously, it was found that for coated systems that still at depths where the film or substrate governs the behavior (corresponding to $R2$ and $R4$ regions on figure 4), the data behavior is better adjusted by a $P-h^{1.5}$ rather than $P-h^2$ plots.

Figures 7 to 9 shows typical $P-h^{1.5}$ and $P-h^2$ plots for every one of these regions. Figure 7(a) shows $P-h^2$ plots for both systems at 50 mN, at this load level the behavior corresponds to a $R2$ region, each of these plots are the same for both systems, indicating that the response is only due to the film, and the substrate has not any contribution. Again, $P-h^{1.5}$ plots (figure 7 (b)) are almost linear. In fact, the correlation coefficients of adjusted lines are better than those obtained in $P-h^2$ plots. The end of this region is shown as Tc/s in these Figures. For both systems, $P-h^2$ and $P-h^{1.5}$ predict this transition at 50 mN. This is better illustrated in Figure 8. Note how $P-h^{1.5}$ plots present the best correlation coefficients for $R1$ and $R2$ regions, while $P-h^2$ are linear for the $R2$ portion but not for $R1$. The RID parameter at this load level is equal to 0,07. The fact that both systems have the same Tc/s tells that at least for a couple substrates

used here the substrate plastic deformations, at this load level, did not play an important role in film's deformation. Also the RID value confirms the rule of thumb of "not exceed the 10% film thickness to measure its hardness" and also is in the limit proposed by Cay et al [14].

Region $R3$ reflects the influence of film stress relieving, cracking and substrate plastic yield. In the case of $TiN-304L$ the first pop-in occurs at 85 mN, and for $TiN-M2$ this event occurs only until 110 mN. This phenomenon seems not to be an evidence of cracking, because topographical images obtained by AFM does not show any annular crack at loads little higher than these.

Note that the substrate contributions begin before the first pop-in, this does not exclude the possibility of film microcracking, subsurface cracking and densification, but this could not be verified in this work because physical sections of the imprints could not be obtained. The fact that the systems go from $R2$ to $R3$ region before the first pop-in occurs, means that the films are following the substrate plastic deformation. This explains why the $TiN-M2$ delay the first pop-in, and is because $M2$ steel is harder than the $304L$ steel, therefore this last will reach first higher deformation levels, producing also high deformations on the film.

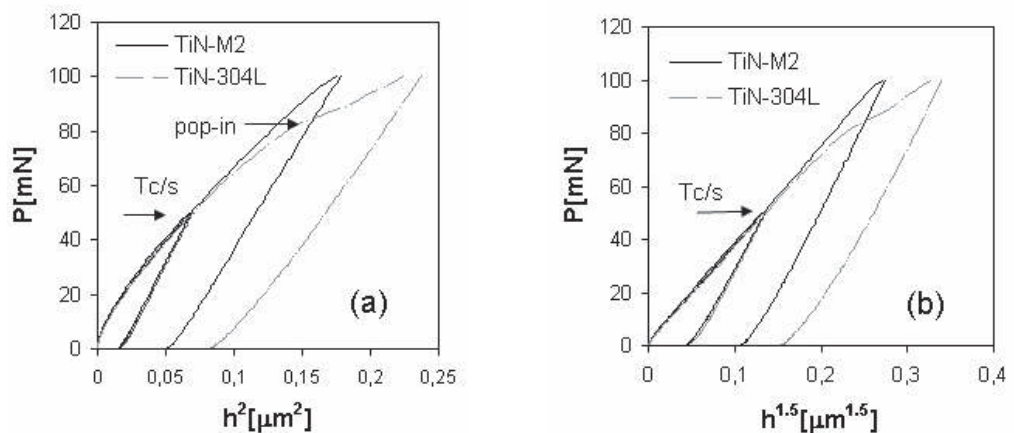


Figure 7 $P-h^2$ and $P-h^{1.5}$ plots for $TiN-304L$ and $TiN-M2$ systems obtained at 50 mN and 100 mN. Tc/s denotes the transition points from $R1$ region to $R2$ regions

After these first *pop-ins*, still in *R3* region, more of them occur and are detectable, in some cases they are associated with different crack types, and are extensively discussed in references [2, 14-16].

Micrographs in figures 10 and 11 at different load levels shown that *TiN-M2* system is less prone to suffer cracking than *TiN-304L* system. *TiN-M2* systems at loads greater than the maximum achievable by the nanoindenter equipment, for example at 300 gf, seems to display only superficial cracks, while *TiN-304L* system clearly shows circular cracks that probably propagate through thickness. Due to that the *M2-TiN* system for all loads in nanoindentation range have contribution of the coat to support load, $P-h^n$ plots do not show a clear transition points, to only substrate behavior, contrary to what occurs in *TiN-304L* system.

Figure 8 shows the end of *R3* regions as Ts/s , and are summarized in table 1. By what was discussed above, it is expected that the system with a harder substrate delay its transition more than the system with soft substrate [14], at least the load at which it occurs. The transition point obtained from the *RID* plot was defined as the point in which the plot has a change in curvature before reaching the plateau called here *RID**. These results were in agreement with what was expected. However, the results of $P-h^2$ plots contradict this expectation, also transition points are variable with the maximum load used for the analysis. Therefore, the results reported here come from plots obtained at maximum load of 1000 mN allowed by the equipment. On the other hand $P-h^{1.5}$ plots predictions are according to the expectation. The best correlation coefficients for plateau regions in plots $P-h^{1.5}$ compared with those of $P-h^2$ plots strongly suggest that $P-h^n$ plots are more convenient to find the transition points. However, it must be pointed out that slightly deviations from the correct frame compliance or area function of nanoindenter could influence the $P-h^n$ plot's shape, and Fishercope equipments seems to have a variable frame compliance, currently we

are conducting studies to solve this question. Yet, it could be concluded that as a whole $P-h^2$ and $P-h^{1.5}$ plots shown to be difficult for discern the transition points because it is necessary to define the minimum correlation coefficient at which one considers that the adjusted plots for plateau regions are straight lines. Consequently, it is possible to obtain different transition point values for little differences in correlation coefficients; this is particularly true for coatings under hard substrates.

On the other hand, the efficiency parameter β_o obtained from *RID* plots showed in table 1 indicate that in fact *TiN-304L* system has less capacity to support loads, i. e. $\beta_o = 0,22$ while for *M2-TiN* systems $\beta_o = 0,27$. An advantage of the β_o parameter is that it permits to compare different film-substrate systems, because it seems to be more sensible than the η parameter of the $P-h^n$ plots. Also, it was not necessary to make assumptions to find the β_o parameter, because it comes directly from *RID* plots. Finally *RID** parameter has the advantage that it is easy to find out, but at least without a computational routine is prone to subjectivity and different systems could be non-comparable contrary to the case of β_o parameter.

Figure 4 shows χ and k parameters obtained from the *RID* plots. χ values according to Tuck [6] are related to the system load support capacity, in this work it was found that χ seems not too sensible to the response of the systems because its values were 2,6 for both of them.

Taking into account that *RID* plots show different behaviors for both systems, it is possible to conclude that χ parameter is not useful to describe the systems under study. In fact, when a value of 2 was fixed for this parameter (as the first developments of the model proposed [1]), the model also produces a good fit.

On the other hand, the k parameters were equal to 30 and 20 for *TiN-304L* and *M2-TiN* systems respectively. According to Tuck [6] this parameter is related to the system deformation mode. High

Table 1 Transition points Ts/s obtained by P-h², P-h^{1.5} and RID plots

sample	RID						P-h ² (L)			P-h ^{1.5}		
	P	RID*	h	P	β_0	h	P	RID	h	P	RID	h
	[mN]		[μm]	[mN]		[μm]	[mN]		[μm]	[mN]		[μm]
TiN-304L	245	0.4	1.22	130	0.22	0.65	400	0.85	2.6	200	0.33	1.08
TiN-M2	580	0.5	1,48	250	0.27	0.82	380	0.23	0.7	380	0.32	1.09

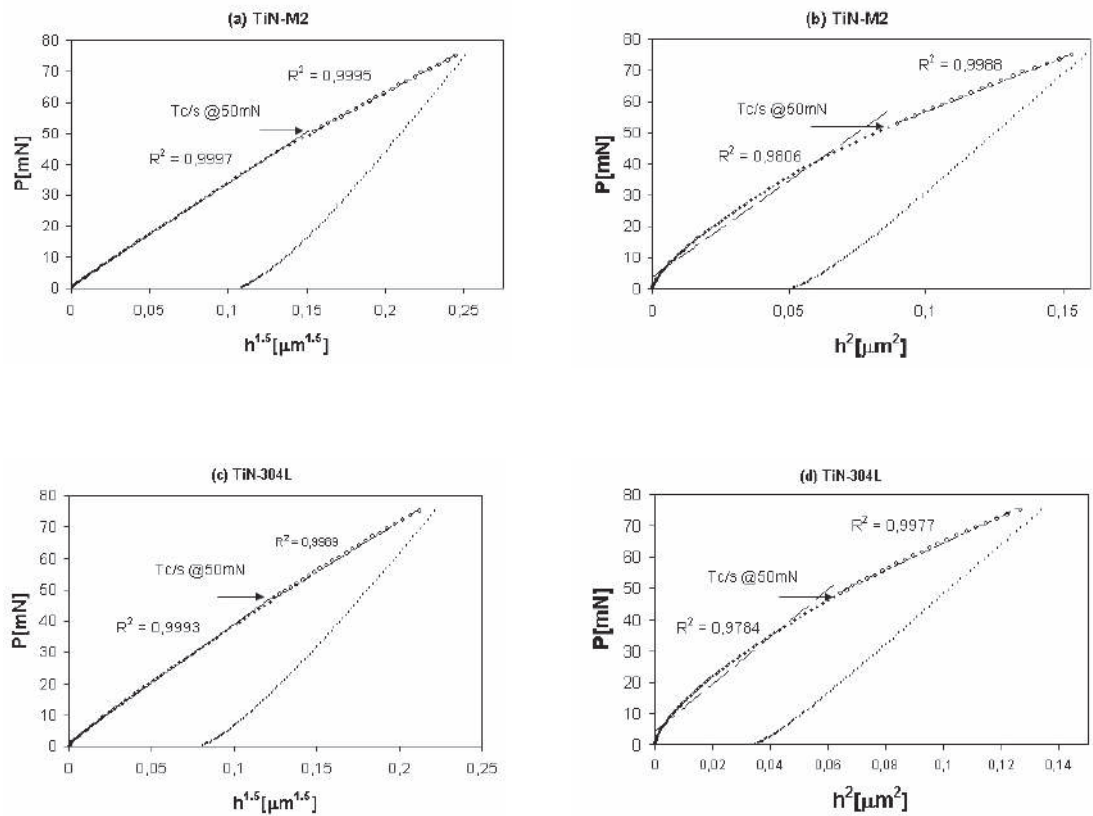


Figure 8 P-h^{1.5} and P-h² plots obtained at 70 mN for both systems. Arrows marked as Ts/c denote the load transitions from film response (*R1* region) to film-substrate response (*R2* region). Also correlation coefficients of the lines adjusted to a *R1* and *R2* region are denoted as R^2

values of it correspond to a soft substrate and high fracture toughness. According to this, the *M2-TiN* system has less fracture toughness but better load support capacity (it substrate is harder).

In *R3* region, for both systems, cracks seem to be superficial, as is shown in figures 10 and 11.

These Figures shows that these cracks have shear steps shape. As the load is increased, first annular cracks are originated and are visible at the edge and inside the indentation, particularly for *TiN-304L* system probably at loads about 0,5 *RID* they are trough thickness, however can not be possible to obtain sections of them to confirm this.

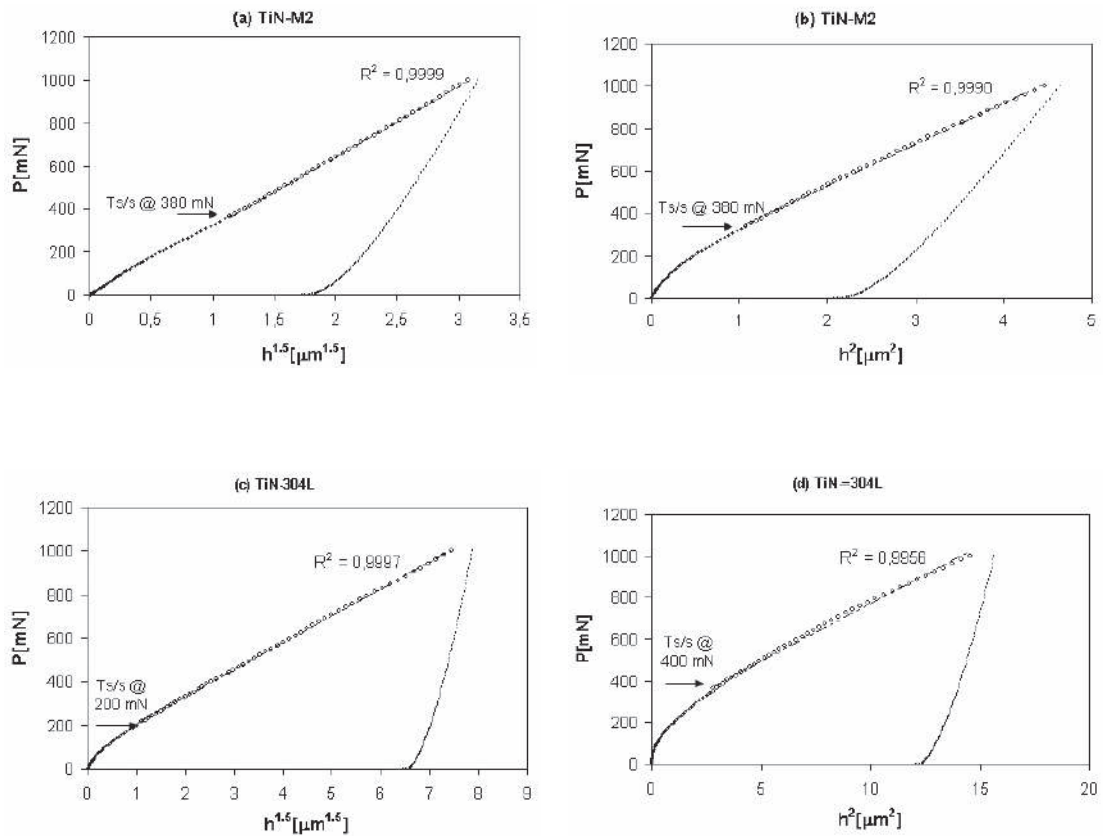


Figure 9 P-h^{1.5} and P-h² plots obtained at 1.000 mN for both systems. Arrows marked as Ts/s denote the load transitions from film-substrate response (*R2* region) to only substrate response (*R3* region). Also correlation coefficients of the line adjusted to a *R3* region are denoted as R²

Finally the *R4* region for *TiN-304L* show a response due almost exclusively to substrate whose pile-up contributes to an extensive coating cracking, in this case a complete annular crack is present, which means that coating has no influence in system behavior. For hard substrate almost all cracks seems to be very superficial and the coating still influences the system behavior.

At high loads first radial cracks are produced and the critical load to generate them are lower in *M2-TiN* (at 5Kg) than in the *TiN-304L* system (at 10 Kg). Also the radial cracks were always longer in *M2-TiN* system. This indicates that the elastic recovery plays an important role in the generation of this type of cracks as for the case bulk materials [17], and strongly suggest that

the films K_c hardly could be obtained by this method because substrate began to suffer plastic deformation and play an important role on the contact system response. However, this behavior match with the conclusions derived from k parameter, because radial cracks length and density are great for brittle systems. This suggests that energy techniques must be explored to obtain

more information about the fracture behavior of brittle coated systems.

At the end of R_4 region, the extensive coating cracking causes that the coatings only transmit load and the properties measured corresponds only to a substrates, which have an elastic modulus of 250, 220 GPa and a harness of 7,8 2,5 GPa for the M2 and 304L steels respectively.

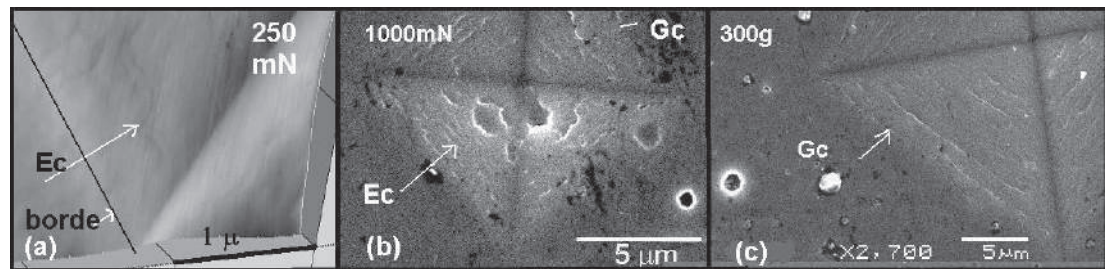


Figure 10 (a) AFM image for imprint leave at 250 mN for *TiN-M2*, arrow indicates the shear steps (Ec). (b) y (c) SEM images for imprints leave at 1.000 mN and 300gf respectively, arrows marked as Gc show circular cracks T

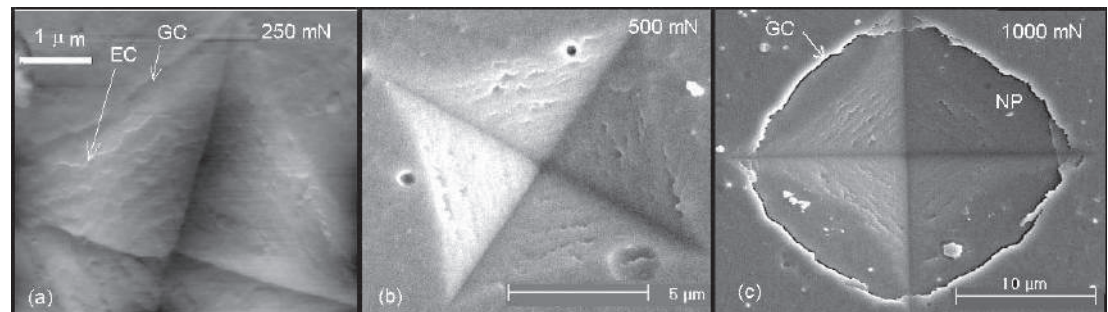


Figure 11 (a) AFM image for imprint leave at 250 mN for *TiN-304L*, arrow indicates the shear steps (Ec) (b) y (c) SEM images for imprints leave at 500 mN and 1.000 mN respectively, arrows marked as Gc show circular cracks

Conclusions

The hardness of *TiN-M2* and *TiN-304L* samples show the so called *ISE* effect at low load levels, and seems to be a morphological, structural-film effect and a geometric indenter effect.

$P-h^{1.5}$ plots fit better the plateau intervals for film or substrate only response than the $P-h^2$ plots.

Therefore, $P-h^n$ plots are more conveniently to find the transition points than $P-h^2$ plots. Nonetheless, from both plots it is not easy to find this transition points due to the sensibility of the adjusted lines to acquired data and to its dependence with the maximum load used for the analysis. Also hard substrates hide transition points in these plots, and results from both plots are very different.

RID plots can provide a great deal information about mechanical responses of coated systems. In particular, the *efficiency parameter* β_o , is more suitable than $P-h^n$ plots to establish the transition points. This parameter could be used to compare different sort of systems, and should be a powerful design parameter. Also k parameter obtained from this plots seems to provides important information about to fracture process.

Superficial cracks generated at low load levels are of the shear steps type, for the films under study they seem not to be through thickness. With load increasing, circular cracks are generated, and some of them could be through thickness, they conduct to a loss of film stiffness and therefore to a loss in the capacity to support load until the substrate is the only responsible of it.

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