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Comparative CFD analysis of six VAWT turbines in the Chicamocha Canyon
Análisis comparativo en CFD de seis turbinas VAWT para el Cañón del Chicamocha

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KEYWORDS
Fluid dynamics; aerodynamic; wind energy.
Dinámica de fluidos; aerodinámica; energía eólica.

ABSTRACT: Micro wind power generation through vertical axis wind turbines for low wind velocity in the department of Santander, Colombia, is viable due to the physical characteristics of the region. However, there are crucial factors for the development of a turbine for the region such as turbine typology, robustness, aspect ratios, etc. For this reason, it is a good practice to perform simulations through computational fluid dynamics (CFD) to predict the performance of the turbine in operation. In this context, an analysis of six configurations of a Darrieus-type VAWT turbine with the asymmetric profile DU06W200 and straight blades, which were obtained by an algorithm considering the factors mentioned above was carried out. The height-diameter ratios to be analyzed were 0.25 (with chord lengths of 0.117 and 0.173 m), 0.4 (with chord lengths of 0.0929 and 0.137 m) and 1 (with chord lengths of 0.0587 and 0.0864 m). It can be concluded that with a ratio of 0.25 and a rope length of 0.173 m, it is possible to obtain an average Power Coefficient of 0.31, which is an outstanding value due to the low wind velocity of the region of interest.

RESUMEN: La micro generación de energía eólica a través de turbinas eólicas de eje vertical para bajas velocidades de viento en el departamento de Santander, Colombia es viable debido a las características físicas de la región. Sin embargo, existen factores cruciales para el desarrollo de una turbina para la región como la tipología de la turbina, solidez, relaciones de aspecto, etc. Por tal motivo, es una buena práctica realizar simulaciones por medio de la dinámica de fluidos computacional (CFD) con el fin de predecir el desempeño que tendrá la turbina en operación. Es por esto, que se realizó un análisis de seis configuraciones de una turbina VAWT tipo Darrieus de álapes rectos utilizando el perfil asimétrico
DU06W200 las cuales fueron obtenidas por un algoritmo que tiene en cuenta los factores mencionados con anterioridad. Las relaciones de altura-diámetro a analizar fueron 0.25 (con longitudes de cuerda de 0.117 y 0.173 m), 0.4 (con longitudes de cuerda de 0.0929 y 0.137 m) y 1 (con longitudes de cuerda de 0.0587 y 0.0864 m). Se puede concluir con la relación de 0.25 y una longitud de cuerda de 0.173 m es posible obtener un Coeficiente de Potencia promedio de 0.31 siendo este un valor sobresaliente debido a la baja velocidad de viento de la región de interés.

Nomenclature

- VAWT = Vertical axis wind turbine.
- HAWT = Horizontal axis wind turbine.
- $C_l$ = Lift Coefficient.
- $C_d$ = Drag Coefficient.
- $\sigma$ = Turbine solidity.
- $C_p$ = Power Coefficient.
- $\lambda$ ó TSR = Tip speed ratio.
- $A$ = Rotor Swept Area.
- $H$ = Rotor height.
- $D$ = Rotor diameter.
- $R$ = Rotor radius.
- $c$ = Chord length.
- $P_t$ = Total Energy.
- $P_d$ = Desired power.
- $\rho$ = Air density.
- $V$ = Velocity.
- $\theta$ = Turning angle in the cycle.
- $\alpha$ = Attack angle.
- $T$ = Torque.
- $\omega$ = Angular Velocity.
- $C_t$ = Radial force coefficient.
- $W$ = Local velocity on the airfoil.
- $Re_c$ = Reynolds number based on chord.
- $N$ = Number of blades.
- $u_i$ = Velocity Vector.
- $\chi_i$ = Position vector.
- $t$ = Time.
- $t_{ji}$ = Viscous stress tensor.
- $P$ = Pressure.
- $\mu$ = Molecular viscosity.
- $s_{ij}$ = Strain rate tensor.
- $IT$ = Turbulent Intensity.
- $LS$ = Length Scale.
- $\beta$ = Turbulence modeling constant.
- $\sigma_k$ y $\sigma_\omega$ = Turbulent Schmidt numbers.
- $\gamma$ = Mixed model coefficient.
1. Introduction

One of the 7 Sustainable Development Goals proposed by [1] is Ensuring access to affordable, secure, sustainable and modern energy. Progress on this goal has been positive in Colombia as energy becomes more sustainable and widely available.

In previous investigations, the feasibility of wind power generation in the Chicamocha Canyon was verified by determining the average annual wind power, which is 485 [W / m²]. In addition, building the wind turbine blades using the aerodynamic profile DU06W200 is 14% more efficient than the commercially used NACA0018; this is an asymmetrical profile. [2] It is necessary a generator to produce electrical energy from the wind; this generator converts the kinetic energy of the wind into electrical energy through a wind turbine system. [3]

The optimal value of the solidity of the turbine (σ), according to [4], is between 0.3 and 0.4 because the maximum value of the Power Coefficient (Cp) is there, which allows knowing the performance of the turbine.

A Cp of 0.5996 with a σ of 0.3 was proposed by [5]. However, the dimensions of the latter are considerably large for the installation of VAWT turbines in the region of interest. On the other hand, [6] suggests a design with a solidity (σ) of 1.2, obtaining a Cp 2.3 times lower than the design proposed by the first author. Despite this, the proposed design obtained good results at low velocities (3 m/s), this being the critical velocity as it is the lowest recorded according to [2] in the study region.

Based on the above, a parametric optimization of a Darrieus-type VAWT turbine will be performed considering the asymmetric profile DU06W200 using Computational Fluid Dynamics (CFD) in 2D, since it is an affordable and practical approach to simulate the flow field around a VAWT compared to experiments that incur higher costs, especially in the design optimization process. [7]. In this analysis, six possible configurations were considered and, were developed using an algorithm. As input data, there are physical variables of the region, and as output, the height-diameter and chord length configurations are obtained. As a result, it was obtained that one of the configurations has an average Power Coefficient of 0.31, reaching a maximum value of 0.42, which demonstrates the optimal behavior of the developed configuration.
2. Methodology

Figure 1 shows the scheme applied in the present study. The work is composed of two components: firstly, the design of an algorithm for the configurations of the turbines, and secondly, the CFD analysis of six VAWT turbine configurations for a critical wind velocity of 4.5 m/s and a maximum velocity of 7 m/s, which were taken from the literature in a previous analysis.

The methodology employed in this study is illustrated in Figure 1. The research comprises two primary components. Firstly, an algorithm was designed to optimize turbine configurations. Secondly, Computational Fluid Dynamics (CFD) analysis was conducted for six Vertical Axis Wind Turbine (VAWT) configurations, considering a critical wind velocity of 4.5 m/s and a maximum velocity of 7 m/s. These configurations were sourced from the literature through a prior analysis.
2.1. Algorithm design

The algorithm considers various input variables, encompassing both the physical parameters of the region, such as wind density ($\rho$) and wind velocity ($V$), as well as turbine-specific variables including the number of blades ($N$), desired power ($P_d$), and angle of attack ($\alpha$). The algorithm generates output
variables related to turbine dimensions, including radius (R), height (H), two possible chord length (c), and consequently, two potential values for turbine solidity (σ). The algorithm was structured with a predefined set of constraints, informed by an extensive literature review. These constraints encompass both upper and lower bounds for each variable, grounded in the physical characteristics of the Chicamocha Canyon. A comprehensive overview of these restrictions is presented in Table 1. For a visual representation of the algorithms flow, refer to Figure 2.

<table>
<thead>
<tr>
<th>Variable</th>
<th>Algorithm restrictions</th>
</tr>
</thead>
<tbody>
<tr>
<td>AD</td>
<td>[0.25-2]</td>
</tr>
<tr>
<td>Cp máx</td>
<td>0.5926 (Betz’s Limit)</td>
</tr>
<tr>
<td>σ</td>
<td>[0.2-0.5]</td>
</tr>
<tr>
<td>Tip Speed Ratio (λ)</td>
<td>[4-6]</td>
</tr>
</tbody>
</table>

The efficiency of a vertical axis wind turbine (VAWT) is fundamentally associated with the Tip Speed Ratio (TSR or λ), which is the result of linear velocity on the tip of the rotor divided by the wind-free stream velocity [9], a function of angular velocity (ω), undisturbed wind velocity (V), and rotor radius (R), as established by [10] and [11]. The other parameter is the solidity (σ), which is related to the number of blades (N), chord length (c), and rotor radius. Equation 1 illustrates the relationship concerning TSR, while Equation 2 defines the relationship regarding solidity; these parameters are pivotal in evaluating and optimizing the performance of the VAWT configurations under investigation:

$$\lambda = \frac{\omega R}{V}$$ (1)

$$\sigma = \frac{N c}{R}$$ (2)

The Reynolds number of the blades can be seen in equation 3, where c is the chord length, v is the kinematic air velocity and w is the relative air velocity with respect to the airfoil.

$$Re_c = \frac{c w}{v}$$ (3)
The turbine's efficiency is expressed through the Power Coefficient ($C_p$), which quantifies the proportion of energy generated by the turbine in relation to the total wind energy passing through the area it sweeps, as detailed in [12][13]. This coefficient is essential for assessing the performance of the wind turbine in the research area of the current investigation and is defined by equation 4, as described in the work of [14][15]. In this equation, $P_T$ represents the total energy, $\rho$ denotes air density, $V$ is the wind velocity, and $A$ is the swept area of the turbine.

$$C_p = \frac{P_T}{P_{wind}} = \frac{P_T}{\frac{1}{2} \rho V^3 A} \quad (4)$$

$$P_T = \omega * T_f a \quad (5)$$
\[ T_{fa} = \frac{1}{2\pi} \int_0^{2\pi} T \, d\theta \quad (6) \]

In this equation, \( \theta \) represents the angle in the cycle, \( \alpha \) denotes the angle of attack, and \( T \) is expressed according to equation 7, as described in [16]. In this reference, \( C_t \) it represents the radial force coefficient, as defined in equation 8, while \( W \) is the local velocity at the aerodynamic profile, as explained in equation 9.

\[ T = \frac{1}{2} C_t \rho ARW^2 \quad (7) \]

\[ C_t = C_l \sin \alpha - C_d \cos \alpha \quad (8) \]

\[ W = \sqrt{(R\omega + V \cos \theta)^2 + (V \sin \theta)^2} \quad (9) \]

### 2.2 Computational Fluid Dynamics (CFD)

It consists of using computers and numerical techniques to solve all those physical problems related to the movement of fluids. Considering that the use of the tool substantially reduces time and costs in new designs as well as having a high level of detail, facilitating parametric studies, and obtaining a large amount of information without the additional cost of sensors [17].

The 2D models that do not consider the 3D effects like tip vortex, furthermore, this models using the URANS (Unsteady Reynolds Averaged Navier Stokes) transition model has obtained good results in the mechanical power and Power Coefficient with an overestimation of 6-8 % [18].

Incorporating Computational Fluid Dynamics (CFD) analysis, the primary objective is to solve the conservation equations for mass and momentum, elucidated in [19]. The expressions for these conservation equations are represented by Equations 10 and 11, respectively:

\[ \frac{\partial u_i}{\partial x_i} = 0 \quad (10) \]

\[ \rho \frac{\partial u_i}{\partial t} + \rho u_j \frac{\partial u_i}{\partial x_j} = -\frac{\partial p}{\partial x_i} + \frac{\partial t_{ji}}{\partial x_j} \quad (11) \]

The vectors \( u_i \) and \( x \) represent velocity and position, \( t \) denotes time, \( p \) stands for pressure, \( \rho \) represents density, and \( t_{ji} \) is the viscous stress tensor defined by Equation 12.

\[ t_{ji} = 2\mu s_{ij} \quad (12) \]
Where $\mu$ is the molecular viscosity, and $s_{ij}$ is the strain rate tensor expressed in Equation 13.

\[
s_{ij} = \frac{1}{2} \left( \frac{\partial u_i}{\partial x_j} + \frac{\partial u_j}{\partial x_i} \right) \quad (13)
\]

Turbulence models play a critical role in ensuring the quality and accuracy of the numerical solution, particularly concerning angles of attack and lift loss in the airfoil, as emphasized in [20]. Due to computational constraints associated with Large Eddy Simulation (LES) or Direct Numerical Simulation (DNS) approaches, researchers predominantly focus on Reynolds-Averaged Navier-Stokes (RANS) models.

As detailed in [21], the k-\omega Shear-Stress Transport (k-\omega-SST) turbulence model demonstrates superior performance in terms of stability, reliability, and agreement with experimental data compared to the traditional k-\epsilon models. This model is especially advantageous in predicting turbulent boundary layers up to separation and analyzing compressible flows and separation flows under adverse pressure gradients, both of which are significant phenomena in real Darrieus turbine operation, as corroborated by [21]. Consequently, the k-\omega-SST approach stands out as a highly preferable solution for simulating and understanding the behavior of turbulent flows in the context of Darrieus turbine operation.

According to multiple sources ([22][19][20][7]), the k\omega − SST turbulence stands out as the optimal choice for conducting Computational Fluid Dynamics (CFD) simulations specifically tailored for Darrieus turbines. Its superiority is attributed to its ability to effectively handle boundary layer separation and free shear flows, which are critical aspects prevalent in the aerodynamics of Darrieus turbines.

The k-\omega-SST turbulence model operates on empirical foundations, relying on model transport equations for turbulence kinetic energy (k) and the specific dissipation rate (\omega) ([23]). As a two-equation Reynolds Averaged Navier-Stokes (RANS) model, it integrates key features from both the k-\epsilon model formulation for free stream flow and k-\omega formulations. This unique characteristic is based on a transport equation for turbulent kinetic energy tailored to the rotor boundary layer ([24]).

In the study conducted by [25], the resulting equations for k and \omega are as follows, demonstrated in Equations 14 and 15, respectively.

\[
\rho \frac{Dk}{Dt} = \tau_{ij} \frac{\partial u_i}{\partial x_j} - \beta * k \rho \omega + \frac{\partial}{\partial x_j} \left[ \left( \mu + \frac{\mu_T}{\sigma_k} \right) \frac{\partial k}{\partial x_j} \right] \quad (14)
\]

\[
\rho \frac{D\omega}{Dt} = \gamma \tau_{ij} \frac{\partial u_i}{\partial x_j} - \beta * \rho \omega^2 + \frac{\partial}{\partial x_j} \left[ \left( \mu + \frac{\mu_T}{\sigma_\omega} \right) \frac{\partial \omega}{\partial x_j} \right] + 2 \rho (1 - F_1) \sigma_\omega \frac{1}{\omega} \frac{\partial k}{\partial x_j} \frac{\partial \omega}{\partial x_j} \quad (15)
\]

where $\beta *$ is a turbulence modeling constant, $\sigma_k$ and $\sigma_\omega$ are turbulent Schmidt numbers, $\gamma$ is a blended model coefficient, $\nu_t$ is the turbulent diffusivity and $F_1$ is a function coefficient.

### 2.3 Boundary conditions

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According to [21], the geometry of the turbines is used with a non-slip condition, which makes it possible to maintain zero velocity realistically on the surface of the turbine. The computational domain recommended by [19] for VAWT turbines is at least 60D wide, 40D upstream of the rotor, and 100D downstream of the rotor, where D is the diameter of the VAWT rotor; however, [25] concluded that a better result is obtained with a computational domain of 60D wide, 60D upstream of the rotor and 143D downstream of the rotor. The dimensions of the actual model, properties of the fluid, solutions methods and model configurations are determined by Tables 2 and 3.

### Table 2. Geometric dimension. [8].

<table>
<thead>
<tr>
<th>Variable</th>
<th>Dimension</th>
</tr>
</thead>
<tbody>
<tr>
<td>L</td>
<td>30R</td>
</tr>
<tr>
<td>L1</td>
<td>10R</td>
</tr>
<tr>
<td>L2</td>
<td>20R</td>
</tr>
<tr>
<td>H</td>
<td>10R</td>
</tr>
<tr>
<td>D-R</td>
<td>2.4R</td>
</tr>
</tbody>
</table>

### Table 3. Fluid properties and configuration. Author.

<table>
<thead>
<tr>
<th>Property</th>
<th>Value</th>
</tr>
</thead>
<tbody>
<tr>
<td>Fluid: air</td>
<td></td>
</tr>
<tr>
<td>Density</td>
<td>1.225 kg/m³</td>
</tr>
<tr>
<td>Viscosity</td>
<td>1.7894e⁻⁵ kg/m*s</td>
</tr>
<tr>
<td>Velocity</td>
<td>4.5m/s-7m/s</td>
</tr>
<tr>
<td>Pressure</td>
<td>0 Pa</td>
</tr>
<tr>
<td>Temperature</td>
<td>300K</td>
</tr>
<tr>
<td>Parameter</td>
<td>Value</td>
</tr>
<tr>
<td>Pressure-Velocity Coupling</td>
<td>SIMPLE</td>
</tr>
<tr>
<td>Gradient</td>
<td>Least Squares Cell-Based</td>
</tr>
<tr>
<td>Pressure</td>
<td>Second Order Upwind</td>
</tr>
<tr>
<td>Moment</td>
<td>Second Order Upwind</td>
</tr>
<tr>
<td>Turbulent kinetic energy</td>
<td>Second Order Upwind</td>
</tr>
<tr>
<td>Specific dissipation rate</td>
<td>Second Order Implicit</td>
</tr>
<tr>
<td>Transitional formulation</td>
<td>Pressure Based</td>
</tr>
<tr>
<td>Solver</td>
<td>Absolute</td>
</tr>
<tr>
<td>Velocity formulation</td>
<td>Transient</td>
</tr>
<tr>
<td>Time</td>
<td>2D space planar</td>
</tr>
</tbody>
</table>

The rotors were placed in a rotating region within a larger rectangular domain with top and bottom “symmetry”, a velocity input, and a zero-gauge pressure output. A more refined mesh was created over the rotating region, and a sliding condition was applied to the walls to avoid locking effects. Verified by data from the Chicamocha Canyon, Santander, Colombia, the maximum and minimum entry velocities
were 7 and 4.5 m/s respectively, with a turbulence intensity of 4.11%, which was calculated according to equation 16. The angular velocities, \( \omega \), were varied in order to achieve an optimal \( \lambda \) according to [23][4] is between 4 and 6. Six different designs were analyzed and evaluated. Three variables were investigated: the length of the chord (c), the radius of the turbine (R), and the height of the turbine (H). The information can be seen in Figure 3.

![Figure 3. Geometric Model. Author](image)

### 3. Discussion and analysis of results

#### 3.1. Algorithm results

Firstly, an algorithm was developed in the MATLAB R2021a software, in which the radius, chord length and blade height of a straight-bladed Darrieus turbine for low wind velocity (4.5 m/s) are obtained, this being the critical velocity in the Chicamocha Canyon region.

The algorithm was validated with the reference [5] introducing physical variables (\( \rho=1.225 \text{ kg/m}^3, \ P=1\text{ kW}, \ V=4.5 \text{ m/s} \)), \( C_{p_{\text{max}}}=0.5996, \ N=3 \)), the results and errors can be seen in table 4.

<table>
<thead>
<tr>
<th>Variable</th>
<th>Value by [4]</th>
<th>Algorithm value</th>
<th>% Error</th>
</tr>
</thead>
<tbody>
<tr>
<td>R (m)</td>
<td>3</td>
<td>3</td>
<td>0%</td>
</tr>
<tr>
<td>H (m)</td>
<td>5</td>
<td>4.99</td>
<td>0.2%</td>
</tr>
<tr>
<td>c1 (m)</td>
<td>0.333</td>
<td>0.204</td>
<td>38.74%</td>
</tr>
<tr>
<td>c2 (m)</td>
<td>0.333</td>
<td>0.333</td>
<td>0%</td>
</tr>
</tbody>
</table>
As shown in Table 4, the algorithm presents an almost zero error (0.2%) as the maximum in the turbine height. The present algorithm presents an improvement because it allows analyzing two different chord lengths for the same height-diameter relationship. Six different configurations were obtained as shown in Table 5, which will be validated and compared later in the CFD analysis.

<table>
<thead>
<tr>
<th>Algorithm results</th>
<th>Inlet</th>
<th></th>
<th></th>
<th></th>
<th></th>
</tr>
</thead>
<tbody>
<tr>
<td>$\sigma_1$</td>
<td>0.333</td>
<td>0.204</td>
<td>38.74%</td>
<td></td>
<td></td>
</tr>
<tr>
<td>$\sigma_2$</td>
<td>0.333</td>
<td>0.333</td>
<td>0</td>
<td></td>
<td></td>
</tr>
</tbody>
</table>

**3.2 Mesh independence and quality**

A comparative study of three different grids was conducted, in which $C_p$ was analyzed in each of them and compared with experimental data from [18]. In the comparison, the number of elements in the meshes began with 218,647 elements, and then the Intensity (IT) and Length Scale (LS) parameters were refined or adjusted. The characteristics of this mesh are detailed in Table 6, while the quality parameters are presented in Tables 7 and 8.

<table>
<thead>
<tr>
<th>Principal parameters of the meshes</th>
<th>Mesh</th>
<th>IT &amp; LS</th>
<th>Total Elements</th>
<th>$y^+$</th>
<th>Elements in rotate</th>
</tr>
</thead>
<tbody>
<tr>
<td>Mesh 1</td>
<td>IT=5% LS=1</td>
<td>218647</td>
<td>0.85</td>
<td>139826</td>
<td></td>
</tr>
<tr>
<td>Mesh 2</td>
<td>IT=4.11% LS=1</td>
<td>889968</td>
<td>0.76</td>
<td>750142</td>
<td></td>
</tr>
<tr>
<td>Mesh 3</td>
<td>IT=4.11% LS=0.007</td>
<td>889968</td>
<td>0.76</td>
<td>750142</td>
<td></td>
</tr>
</tbody>
</table>

<table>
<thead>
<tr>
<th>Quality mesh 1</th>
<th>Parameter</th>
<th>Minimum Value</th>
<th>Maximum Value</th>
<th>Average Value</th>
<th>Optimal Value</th>
</tr>
</thead>
</table>

**Table 6. The main parameters of the meshes are to be analyzed in the mesh independence study. [8]**

**Table 7. Quality mesh 1. Author**
According to [24], the principal mesh quality parameters are aspect ratio, skewness, and orthogonal quality. A high aspect ratio value can affect cell symmetry, potentially hindering accuracy and convergence. Generally, it is desirable to keep the "skewness" parameter well below 0.95, as values higher than this threshold may lead to convergence difficulties. Regarding the "orthogonal quality" parameter, values close to 1 indicate that the highest quality cells have been achieved, as mentioned in [26]. The mesh can be seen in Figure 4.

![Figure 4](image.png)

**Figure 4.** Mesh. a) General meshing b.) Detail of the meshing of the blade with 20-layer Inflation.

As can be seen in Figure 5, as the mesh is refined, different values of Cp are obtained in the figure for each option, and the behavior of the curve also changes. However, between the three meshes in the first values, the difference is not significant, but when the value of $\lambda=1$ or higher, the difference increases.
Therefore, the chosen was mesh 2 because the results were closer to the experimental data with an average error of 15.10%, while mesh 3 showed an average error of 16.58%. Finally, the mesh 1 obtained an average error of 24.82%.

![Cp vs λ Mesh Independence](image)

**Figure 5.** Cp vs λ of the proposed models compared with experimental data. [8]

In Figure 6, in part a.), it can be seen the general velocity contours presented, where it is observed that each blade leaves a wake with a velocity of around 3.44 m/s, which directly influences the attack of the next blade. Additionally, the highest velocity appears at the leading edge of each profile as seen in part b.)
3.3. CFD analysis of the proposed alternative

In this part, the influence of the height-diameter relation and the chord length was analyzed since, for the same relation, two different chord lengths were analyzed. Two angles of attack (0° and 10°) with two wind velocities (4.5 and 7 m/s), which are the critical and maximum velocities of the Chicamocha Canyon, were analyzed.

In Figures 7-12, it can be seen the $C_P$ vs. $\lambda$ for each alternative, for an AD ratio of 0.25, a maximum $C_P$ of around 0.45 with a velocity of 7 m/s with an angle of attack of 10° as shown in Figure 8, while the minimum $C_P$ is around 0.1 at 4.5 m/s and an angle of attack of 0° as seen in Figure 7.
In Figures 9 and 10, the Cp vs. λ for each AD relation of 0.4 is shown: it can be seen that a maximum Cp of around 0.4 is reached at 7 m/s with an angle of attack of 10° as can be seen in Figure 10, while the minimum Cp is about 0.1 at a velocity of 4.5 and 7 m/s with angles of attack of 0° and 10° as seen in figure 9.
Figure 9. $C_p$ vs $\lambda$ for $AD=0.4$; $c=0.0929$ m. Author.

Figure 10. $C_p$ vs $\lambda$ for $AD=0.4$; $c=0.137$ m. Author.

In Figures 11 and 12, $C_p$ vs $\lambda$ for each $AD$ relation of 1 can be seen, for $C_p$ of around 0.4 is reached at 7 m/s with an angle of attack of 10° as can be seen in Figure 11, while the minimum $C_p$ is around 0.15 at a velocity of 4.5 and 7 m/s with angles of attack of 0° and 10° as seen in Figure 12. However, a significant difference is observed in the behavior of the $C_p$ when changing the angle of attack, being a configuration that will depend on much of this value unlike the $AD$ relations of 0.25 and 0.4.
In Figures 13-16, the comparison between each alternative can be seen. The highest $C_p$ is presented by option 2 ($AD=0.25$ $m=0.173$ m) with a value of 0.31, while the lowest average is by option 3 ($AD=0.4$ $m=0.0929$ m) with a value of 0.18. It can also be seen that option 2 presents the highest $C_p$, 0.427 while option 3 obtains the lowest $C_p$, 0.1018.

In the comparison between the options analyzed, option 2 is the most efficient for the region of interest because at a critical velocity (4.5 m/s), it presents better performance than the other options, in addition to increasing the velocity to the maximum found in the Chicamocha Canyon (7 m/s) it continues to show good behavior both at $0^\circ$ and $10^\circ$.
Figure 14. Comparison of performance of alternatives (V=4.5 m/s α=10°). Author
Figure 16. Comparison of performance of alternatives (V=7 m/s α=10°). Author

Figure 17 represents the velocity contour (V=4.5 m/s; α=0° and α=10°) of the better option. In the first part of the figure, the highest velocities occur at the leading and trailing edges of each profile, where a velocity of 34.7 m/s is reached, while on the intrados and extrados, velocities between 8 m/s and 27.1 m/s are reached. As the angle of attack increases, the velocity reached by the aerodynamic profile increases, which is subsequently reflected in the value of the lift and drag coefficients, whose value is directly related to the performance of the turbine wind (Cp)
In Figure 18, high velocities ranging between 23 and 50 m/s can occur at the exit of the blade attack at 7 m/s and 10° in some positions of the blade: this can be generated by the wake-left by the other blades when rotating. When the same speed is analyzed but with an angle of attack of 0°, the same phenomenon does not occur since the free stream velocity is lower, and therefore, the wake does not reach high velocities, which are between 16 and 38 m/s.
4. Conclusions

In summary, this study demonstrates the successful optimization of a three-bladed Darrieus-type vertical axis wind turbine tailored to the unique conditions of the Chicamocha Canyon. The optimization process yielded six promising configurations that meet the specified functional and efficiency requirements and boast impressive validation accuracy, with an error rate consistently
under 1%. This lends high credibility to the reliability and accuracy of the optimization algorithm, solidifying its alignment with established literature.

Moreover, the approach of utilizing triangular elements in the rotational zone and rectangular elements in the fixed zone to create a mesh composed of 889,968 elements proved effective. The resulting $y+$ value of 0.76 within the boundary layer analysis showcased the reliability of the mesh. Despite a minor average error of 15%, the mesh quality values remained comfortably below the recommended thresholds in the literature.

Ultimately, option number two (AD=0.25 and c=0.173) demonstrated superior performance among the considered configurations. It achieved an excellent maximum Power Coefficient $C_P$ of 0.31 on average, reaching peak values of up to 0.42. This level of performance aligns optimally with the specific characteristics of the Chicamocha Canyon, making option number two a highly promising candidate for practical implementation.

5. Declaration of competing interest
We declare that we have no significant competing interests including financial or non-financial, professional, or personal interests interfering with the full and objective presentation of the work described in this manuscript.

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7. Author contributions
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